

2.2.3 Dynamic Mass and Weight

1. is a measure of the quantity of matter in an object.

2. in other words,

1. how many molecules
2. how many atoms
- or how many protons, neutrons and electrons.

3. The mass does not change

regardless of where you take it in the universe
→ does not change with a change of state

4. the only way to change mass is to add or take away atoms.

Formula:

$$\text{Mass} = \frac{W}{A} \rightarrow \text{weight} \quad \text{gravity}$$

$\text{gravity} = \frac{32.2}{\text{ft/s}^2}$

Example:

$$W = 32.2 \text{ lbs/s}$$

$$W = 32.2 \text{ lb}$$

$$m = ?$$

$$m = \frac{W}{A} = \frac{32.2}{32.2} = 1 \text{ slug}$$

object more mass
↑ has
more inertia
than lesser object
for example
sand in bucket

For example, if we apply force for an object, the tendency will be for the object to move.

For work, power, torque to exist there has to be a force that initiates the process.

GE-90's turbofan engine, Powerplant for Boeing 777-300
Pounds of thrust = 115000

Inertia:

1. is a resistance of an object to change its state of motion, including changes to its speed or direction

2. Inertia tend to keep an object moving in a straight line and constant speed velocity

3. Inertia is a property, needs to be overcome before a stationary body may begin to move from its present position

4. The object will continue moving at its current velocity, until force causes its speed or direction to change.

Unit of the force, Pound (lb) and Newton (N)

When we thrust the turbine engine we use $F = m \times a$ and thrust expressed in Pound (lb)

$$1 \text{ lb} = 4.448 \text{ N}$$

Slugs is a quantity of mass.

$$\text{gravity} = 32.2 \text{ ft/s}^2$$

Mass of 1 slug = 32.2 lb

Weight

1. is a measure of the pull of the gravity acting on the mass of an object

2. The more mass an object has, the more it will weigh under the earth's surface of gravity.

3. The only way for an object to be weighed is for gravity to go away.

4. it is not possible for the mass to go away of object

Formula:

$$W = m \times \text{Gravity}$$

Force:

1. is intensity of impetus
2. or intensity of an impulse

Work:

- The study of machine both simple and complex, is in one sense a study of energy of mechanical work
- this is true because
- All machine transfers input energy
- Work done on the machine
- to output energy
- Work done by machine

WORK: is done when a resistance is overcome by a force acting through a measurable distance.

Example:

A small aircraft stuck in snow. The two men push against it for a period of time but the aircraft not move. So no work is done in pushing against aircraft $W = 0$

Work: is accomplished only when an object is displaced some distance against a resistive force

Formula:

work = Force $\times$ distance

$$W = F \times d \rightarrow \text{linear distance}$$

Imperial system: $F \rightarrow \text{lb}$
 $d \Rightarrow \text{feet or in}$

So $W \Rightarrow \text{foot-pound or inch-pound}$

Metric system: $F \Rightarrow \text{N}$
 $d \Rightarrow \text{m}$

$W \Rightarrow \text{Joules}$

$$1 \text{ lb Force} = 4.448 \text{ N}$$

$$1 \text{ m} = 3.28 \text{ ft}$$

$$1 \text{ J} = 1.36 \text{ ft-lb}$$

Example:

$$W = ??$$

$$W = F \times d$$

$$F = 150000 \text{ lb} = 150000 \times 3$$

$$d = 3 \text{ ft} \quad \frac{150000}{3} = 45000 \text{ ft-lb}$$

refer to the book $P = (2.20)$, last Example of the work:

$F \neq W$ of airplane. Because the airplane being moved horizontally and not lifted vertically. In all cases, it takes less work to move something horizontally than it does to lift it vertically.

Power:

- Force being applied over a measured distance add one more thing over time
- How long does it take to accomplish the work
- if weight is to be lifted in a shorter period of time, it will take more power

Formula:

$$\text{Power} = \frac{\text{Force} \times \text{Distance}}{\text{Time}}$$

$$P = \frac{F \times d}{t}$$

$$P \Rightarrow \frac{\text{ft-lb}}{\text{min}}$$

$$\frac{\text{ft-lb}}{\text{s}}$$

$$\frac{\text{in-lb}}{\text{min}}$$

$$\frac{\text{in-lb}}{\text{s}}$$

depend how distance and time are measured

horsepower = 550 ft-lb/s (hp)

to convert power to horsepower, follow

$$1 \text{ hp} = 550 \text{ ft-lb/s}$$

$$1 \text{ hp} = 33000 \text{ (ft-lb/min)}$$

$$1 \text{ hp} = 375 \text{ mi-lb/hr}$$

$$1 \text{ hp} = 746 \text{ watts (electricity conversion)}$$

divide the power by

appropriate conversion

38000 based on the unit given

$$\frac{2 \times 76000}{6}$$

$$\frac{319000}{76000}$$

Example:

$$P = \frac{F \times d}{t}$$

$$d = 4 \text{ ft} \quad = \frac{140000 \times 4 \text{ ft}}{2 \text{ min}} = \frac{140000}{2}$$

$$t = 2 \text{ min} \quad \text{power} \quad = \frac{38000 \text{ ft-lb/min}}{2 \text{ min}} = 19000$$

$$F = 19000 \quad \text{Hp} = \frac{38000}{33000} = 1.15$$

Torque:

as we know, work is force acting through a distance.

Torque:

- Force acting along a distance
- is something that creates twisting and tries to make something rotate.

Example of work

= push object

but torque like wrench, bolt.

Formula:

$$\text{Torque} = \text{Force} \times \text{Distance}$$

$$T = F \times d \rightarrow \text{torque}$$

Torque:

↳ nothing hard to move, because force being along distance not through distance

↳ the work unit is inch-pounds

↳ the torque unit is pound-inches

some both are different not same.

Example of torque:

→ piston engine

→ gas turbine engine

→ piston engine:

Force in pounds ~~the~~ pushing down on the top of piston and tries to make it move. Piston is attached to connecting rod, which attached to the crankshaft at offset.

Offset: Length of the wrench.

Force: acting on that length won't create torque.

Example:
Force = 500 lbs pushing
offset distance = 4 in
 $T = ??$

$$T = F \times d$$

$$= 500 \times 4$$

$$= 2000 \text{ pound-inches}$$

$$2000 \text{ lbs-in}$$

There is a relationship between
horsepower of engine and
torque of engine

Formula:

$$\text{Torque} = \text{Horsepower} \times \frac{5252}{\text{rpm}}$$

$$T = \frac{HP \times 5252}{\text{rpm}}$$

Example:

engine creates = 180 HP
at 2700 rpm, How many
pound feet of torque is

Horsepower = 180 HP

rpm = 2700 rpm

$$T = ?? = \frac{HP \times 5252}{\text{rpm}}$$

$$= \frac{180 \times 5252}{2700}$$

$$= 350.1333$$

$$= 350.1333$$

$$= 350.1333$$

$$= 350.1333$$

$$= 350.1333$$

Both type create torque
in advance of being able
to create work or power.

Similar to work
ft-lb or in-lb

Energy:

↳ something that gives
capacity to perform
work.

↳ when we said that
we feel full of energy,
means we can perform
a lot of work.

↳ Energy can be
classified as one of two
types:

either potential or kinetic

Potential energy PE

↳ being energy at rest

↳ or energy that is
stored

PE classified into three
groups:

→ that due to position

→ that due to distortion
of elastic body

→ which produce work
through chemical action.

Example due to position:

→ water in an elevated
reservoir

→ airplane raised off the
ground sitting on jacks

Example due to distortion
of elastic body:

→ stretched bungee cord
on a Piper-Tri-Pacer

→ compressed spring.

Example of produce work
through chemical action:

→ aviation gasoline

→ fuel

→ storage batteries

To calculate PE due to position
(height) =

Formula:

$$PE = \text{Weight} \times \text{height}$$

Example:

Weight = 450 000 lb
raised $h = 4$ feet

PE = ??

$$PE = W \times h$$

$$= 450 000 \times 4$$

$$= 1 800 000 \text{ ft-lb}$$

$$= 1 800 000$$

Gasoline has 8 potential
to release heat energy

based on BTU unit
British thermal

$$1 \text{ lb} = 18900 \text{ BTU}$$

each BTU capable of
778 ft-lbs of work

$$1 \text{ lb} = \text{BTU} \times \text{ft-lb}$$

$$= 18900 \times 778$$

$$= 14 704 200 \text{ ft-lb}$$

Kinetic Energy

defined as: in
being energy of motion

Examples:

→ airplane rolling down
the runway

→ rotating flywheel
on an engine

KE: unit

same as PE

foot-pound / inches

Formula:

$$KE = \frac{1}{2} \text{ mass} \times \text{velocity}^2$$

$$KE = \frac{1}{2} m \times v^2$$

show mass as weight
÷ gravity

velocity = feet / s

Example:

Weight = 600 000 lbs

$V = 200 \text{ ft/s}$

KE = ?? ft-lb

$$KE = \frac{1}{2} \times m \times v^2$$

$$= \frac{1}{2} \times \frac{600,000}{32.2} \times 200^2$$

$$= \frac{1}{2} \times 18633.54 \times 40000$$

$$= 372670000$$

$$= 372.67 \text{ MJ}$$

Total energy:

Mechanical energy of an object: can be result of:

→ its motion (KE)

→ its stored energy of position (PE)

Total amount of mechanical energy:

Sum of PE and KE

$$\text{Total ME} = PE + KE$$

$$\text{Total ME} = mgh + \frac{1}{2}mv^2$$

Weight

Heat and Efficiency

Mechanical Efficiency: Require:

the actual performance of a machine to be as close as possible to ideal performance of that machine

In addition of friction losses:

Many machine fail to convert some of the input energy to output due to heat loss.

an engine for example:

loses significant heat energy through conduction to the various parts of the engine.

Not only the combustion of the fuel need to be maximized,

transfer of the energy released must occur with the least amount of heat loss

this is a significant loss for heat engine because

engine, which is turning due heat energy from combustion

is always cooler than heat of combustion and will constantly act as a heat sink.

The most efficient heat engines operate at around 50% efficiency with average engine operating at 25-35% efficiency.

Momentum

Newton third law: "for every action there is an equal and opposite reaction"

is most associated with the force involved in jet engine's thrust.

→ it also applies to the momentum and the actions of the object that are interacting.

there is always:

equal force of opposite direction when an one object act upon another

check example about 2 objects

the momentum will be affected by applied force

Because

force affects acceleration

$F = m \times a$ and acceleration will affect momentum

Newton's 3rd law:

Momentum = $m \times v$

thus, the force of the object will be equal but

their acceleration will be affected differently in relation to their masses.

Conservation of momentum:

1. Even, object 2 is stationary when object 1 applies force to the object 2, so object 2 will accelerate and giving momentum.

2. Object 1 it is already had momentum by its interacting with object 2.

In this case or other case momentum is conserved.

The momentum of each object changes but total momentum of both object remain the same.

Object 2 will accelerate but

object 1 will decelerate but

total momentum of both remain same

this is called conservation of momentum

Impulse :

Force x time = Impulse

Impulse

→ impulse = change in momentum

$$F = m \times a$$

$$a = \frac{\text{Change in Velocity}}{\text{time}}$$

$$F = m \times \frac{\text{change in velocity}}{\text{time}}$$

$$F = m \times \frac{\Delta v}{t}$$

$$Ft = m \Delta v \rightarrow \text{change in momentum}$$

↓ impulse = $m \Delta v$

$$\text{Momentum} = m \times v$$

$$\Delta \text{Momentum} = m \times \Delta v$$

$$\text{Impulse} = \text{change in momentum}$$

$$Ft = m \Delta v$$

Gyroscopic principle

- ply a large role of aviation
- from proper effect on the behavior of aircraft.

↳ Mechanical gyroscope is comprised of a wheel or rotor with its mass concentrated around its perimeter.

↳ The rotor has bearing to enable it to spin at high speed

↳ 2-31A, different mounting configuration

are available for the rotor and axle.

→ which allow the rotor assembly to rotate one or two axes $\perp$ to its axis of spin.

→ to suspend the rotor for rotation, the axle is first mounted in a supporting ring.

2-31B,

If brackets are attached 90° around supporting ring from where the spin axis attached,

→ the supporting ring and rotor can both move freely 360° .

→ When in this configuration the gyro said to be "captive gyro".

→ it can rotate about only one axis that is $\perp$ to the axis of spin.

2-31C

1. Supporting ring can also be mounted inside an outer ring.

2. The bearing point are the same as bracket goes as discussed.

3. Attachment of a bracket to the outer ring allows the rotor to rotate in two planes while spinning.

4. Both of these are $\perp$ to the spin axis of rotor

3-1A gyroscop with this configuration,

two rings + mounting bracket is said to be "free gyro" why:

Because it's free to rotate about two axes that are both $\perp$ to the rotor's spin axis.

2-31D, as a result

Supporting ring with spinning gyro mounted inside is free to rotate turn 360° inside the outer ring.

When rotor is rotated at high speeds, and due to its inertia

The gyro exhibits a unique characteristic. This is called gyroscopic rigidity or rigidity in space.

This means the rotor of a free gyro always points in the same direction no matter which way the base of the gyro is positioned.

Gyroscopic rigidity depend upon several design factor

Weight: For given size, heavy mass is more resistant to disturbing forces than a light mass.

Angular velocity: The higher the rotational speed, the greater the rigidity or resistance to deflection.

Radius at which weight is concentrated:-

Max effect is obtained from a mass when its principle weight is concentrated near the rim, rotating at high speed.

Bearing friction:-

Any friction applies deflecting force to a gyro minimizing bearing friction keeps deflecting force at a minimum.

This characteristic of gyro to remain rigid in space is exploited

→ attitude-indicating instrument

→ directional indicator that use gyro.

Precession:

- > is second important characteristic of gyroscope
- > By applying force to a horizontal axis of the gyro, unique phenomenon occurs
- > The applied force is resisted.
- > instead of responding to the force by moving about the vert axis, the gyro moves in response about its vertical axis.
- This predictable controlled precession of a gyroscope is utilized in a turn and back instrument.
- The rigidity in space and precession characteristic of gyroscope action must always be considered when objects of any appreciable mass are rotating.

Figure 2-33,

When a force is applied to a spinning gyroscope, it reacts as though the force coming from 90° further around the rotor in the direction it is spinning.

-> plane of the applied force, plane of rotation, and plane which the gyro scope response (known as precession) are all $\perp$ to each other.

Friction:

$N = (W)$

A 900 lb is being pulled a distance 200 ft.
-> this it does not mean the work done (Fxd) is 180000

ft-lbs.

Why?

Because the person pulling the load is not working against the total weight of the load, but against the rolling friction of the cart.

Friction:

1. is an important aspect of work.
 2. without friction it would be impossible to walk
 3. is a liability as well as asset and require ~~mechanism~~ consideration when dealing with any moving mechanism
- Measurement of applied force reveals that there are three kinds of friction:

1. one force is required to start a body moving
2. another: keep body moving at constant speed
3. After a body is in motion, large force is required to keep it sliding then to keep it rolling

Three kinds of Friction:

- > Static (static) friction
- > Sliding friction
- > Rolling friction

Static Friction: (at rest) starts

1. When we tried to slide a heavy object on surface, first will broken loose or start, once in motion, it will slide easily.
2. The breaking loose force is proportional to the weight of body.
3. force necessary to start body moving slowly is F.

4. this is normal force presses body against the surface usually ~~DATE~~ weight

coefficient: -

1. nature of the surface
2. designated by letter 'k'.
3. can be established for various materials
4. is often published in tabular form.

if load (weight of object) is known,

starting can be used by this formula:

$$F = k F'$$

↓
coefficient

Example:

$F = 10 \text{ lb}$ $k = 0.3$

-> 

$F = k F'$	0.3
$= 0.3 \times 10$	1.0
$[= 3 \text{ lbs}]$	0.30
	3.0

Sliding Friction:

1. is the resistance to motion offered by an object sliding over a surface.
2. it produces friction after the object has been set in motion.
3. is always less than starting friction

4. The amount of sliding resistance is dependent to the texture of the surface of the object

-> surface over which it is slide

-> Normal force between the object and surface

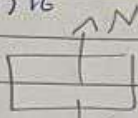
$$F = \mu N$$

No resistance
Force due to
Friction
(pounds) 16

DATE:

Coefficient
of sliding
friction

Force exerted
or objection
to the sum
over which
it slide
(Normal)



one has
no effect
on the
result

$$W = mg$$

16

$$N = mg$$

block = teakwood with
not slide on any side earlier
than other, aren't moving
in the formula

Rolling Friction :-

Resistance to motion :-

is greatly reduced if an object
mounted on wheels or rollers.

Rolling Friction :-

The force of friction for object
mounted on wheels or rollers.

This force :-

may be computed by the
same equation of sliding
friction, but " μ " will be
much smaller.

Example :-

μ for rubber tires or concrete
or macadam ≈ 0.02

The value of " μ " for roller
bearing

is very small, usually ranges
from 0.001 to 0.003 and
often disregarded

Example :- an aircraft with
gross weight 79600 lb is towed
over concrete ramp, what force
must be exerted to get the airplane
rolling after once set in motion

$$\text{Weight} = 79600 \text{ lb} \Rightarrow N$$

$$\mu = 0.002$$

$$F = \mu N$$

$$F = ?$$

$$= 0.002 \times 79600$$

$$159.2 \text{ lb}$$

Coefficient of Friction:

1. is a value that shows
the relationship between

$\rightarrow$ Force of friction

2. between

$\rightarrow$ two objects

3. and the normal reaction
between

$\rightarrow$ The object that involves

It is a value that is
used to

$\rightarrow$ Find an object normal
force

$\rightarrow$ Friction force when
other methods are unknown

Coefficient it can be different
things:

$\rightarrow$ Coefficient of static
friction

$\rightarrow$ Coefficient of kinetic
friction.

$\rightarrow$ Coefficient of static
friction: is the friction

of two objects when neither
of object is moving or
not move

$\rightarrow$ Coefficient of kinetic
friction: is the friction

of two objects when one
object is moving, or both
objects are moving against
one another

Coefficient of friction depend
on

object that are causing
friction.

The value usually between
0 and 1, but can be
greater than one.

0 $\Rightarrow$ means at
there is no friction at
of between objects.

It can be friction only

when two objects touch with
other.

1 $\Rightarrow$ means

friction force is = normal
force

more than 1 means
friction is stronger
than normal force.

A material such
as rubber,

have coefficient
greater than one.

Coefficient of friction

can also be changed
by the mass

$\rightarrow$ and speed of
the moving object