

2.2.4. Fluid Dynamics

Density

1. density of a substance is a weight per unit volume.
2. The unit volume selected for use in the imperial system of measurement is 1 cubic foot (ft^3).
3. In the metric system, it is 1 cubic centimeter (cm^3).
4. density is expressed in (lb/ft^3) or (g/cm^3)

To find density weight and volume must be known

$$\text{density} = \frac{\text{Weight}}{\text{Volume}}$$

Example:- weight 1497.6 lb
contains 4 ft long, 3 wide, 2 ft deep.

$$W = 1497.6 \text{ lb} \quad d = \frac{W}{V} = \frac{1497.6}{24}$$

$$V = 4 \times 3 \times 2 = 24 \text{ ft}^3$$

$$\begin{array}{r} 24 \overline{) 1497.6} \\ \underline{48} \\ 1197 \\ \underline{96} \\ 237 \\ \underline{192} \\ 45 \\ \underline{48} \\ 36 \\ \underline{36} \\ 00 \end{array} \quad \begin{array}{r} 24 \overline{) 1497.6} \\ \underline{48} \\ 1197 \\ \underline{96} \\ 237 \\ \underline{192} \\ 45 \\ \underline{48} \\ 36 \\ \underline{36} \\ 00 \end{array} \quad \begin{array}{r} 24 \overline{) 1497.6} \\ \underline{48} \\ 1197 \\ \underline{96} \\ 237 \\ \underline{192} \\ 45 \\ \underline{48} \\ 36 \\ \underline{36} \\ 00 \end{array}$$

$$= 62.4 \text{ lb}/\text{ft}^3$$

6. The term "specific weight" or "specific density" are sometimes used to express this ratio.
 is not expressed in unit

Formula to find specific gravity of liquid and gas solid:

$$\text{Specific gravity} = \frac{\text{Weight of the substance}}{\text{Weight of equal volume of water.}}$$

$$\text{or} \quad \text{Specific gravity} = \frac{\text{Density of substance}}{\text{Density of water}}$$

The same formula used to find density of gases by substituting air or hydrogen for water.

Example: hydraulic fluid has specific gravity 0.8 ft^3 of liquid weight 0.8 times much 1 ft^3 of water, 62.4 times 0.8, or 49.92 lb

$$\text{Specific gravity} = \frac{0.8}{0.8} = 1 \text{ lb}$$

$$\text{Water: } 62.4 \times 0.8 = 49.92 \text{ lb}$$

$$\begin{array}{r} 62.4 \\ \times 0.8 \\ \hline 49.92 \end{array}$$

specific gravity and density are independent of the size of the sample.

→ change in temperature will not change the weight, but will change the volume. by expansion or contraction, thus changing its weight / unit volume.

Specific Gravity

1. It is often necessary to compare the density of one substance with that of another. For this purpose, a standard is needed.
2. Water is the standard that physicists have chosen to use when comparing the density of all liquids and solids.
3. For gases, air is most commonly used.
4. Hydrogen is sometimes used as a standard for gases.
5. the word "specific" implies a ratio.

6. Specific gravity is calculated by comparing weight of volume of given substance with weight of an equal volume of water.

hydrometer

1. is used for measuring specific gravity of liquids.

2. this device consists of a tubular glass float contained in a large glass tube.

Example :- tubular glass float SG ↑ when immersed in a liquid of greater density, the float rises, indicating a ↑ specific gravity.

-> for liquid of lesser density ↓

The float sinks, indicating lower specific gravity ↓ $\therefore$ ↓ SG ↓ will sink

another example of use of hydrometer electrolyte (battery liquid) in aircraft battery

viscosity :-

- one of the most important properties of fluid is viscosity
- is internal resistance to flow.
- A liquid such as gasoline that has low viscosity flows easily.
- A liquid such as tar that has high viscosity flows slowly.

high viscosity index indicates the fluid experiences small change in viscosity as temperature varies.

The Saybolt Viscometer measures the time required in seconds for 60 ml of the tested fluid at 100°F to pass through a standard orifice.

instrument used to measure the viscosity of a liquid, called known viscometer or viscosimeters.

The time measured is used to express the fluid's viscosity in Saybolt Universal Seconds or Saybolt Furol Seconds.

5. All fluids have viscosity. 6. While easier to see in a liquid, gases, such as air, also have viscosity.

6. In aerodynamics, as air flows over the surface of the aircraft, the viscosity of the air affects the nature of the flow.

7. Viscosity ↑ as temperature ↓ inverse relationship.

Maintaining a functional viscosity throughout the operating temperature range is also an issue in lubricity system.

Viscosity index is a number that indicates the effect of temperature changes on the viscosity of lubricating oil.

Low viscosity index signifies a relatively large change of viscosity during temperature variations.

Fluid resistance :-

- Fluid is any substance that it is able to flow if it's not in some way confined or restricted.
- Liquids and gases are both classified as fluids and often act in very similar ways.
- One significant difference comes into when a force is applied,

Liquids tend to be incompressible
gases tend to be highly compressible

2. theory of WFT on a wing and the force generated by hydraulic system can be explained and quantified by using the law of fluid mechanics.

Pascal's Law

1. he discovered that pressure set up in a fluid act equally in all direction.
2. This pressure acts at right angles to containing surfaces
3. When the pressure in the fluid is caused solely by the fluid's weight, the pressure against the wall of the container is = at any given level but it is not $\neq$ if the pressure at the bottom is compared to the pressure at the top.

1. Concept of the pressure
2. Set up in a fluid
3. how it relates to the force acting on fluid
3. Surface area through which it acts

Relationship between F_{out} and F_{in} is Mechanical Advantage.

$$MA = \frac{F_{out}}{F_{in}}, MA = \frac{D_{in}}{D_{out}}$$

two piston hydraulic system
Relationship between piston area and distance

Formula :-

Input piston Area (Distance moved) = output piston Area (Distance moved)

$$A_{in} \cdot D = A_{out} \cdot D$$

$$Volume_{in} = Volume_{out}$$

Example: A two piston hydraulic system, has input piston an Area $\frac{1}{4} \text{ in}^2$, output piston Area 1 in^2 , input force 50lb, input piston moves 30 in. What is the pressure in system, how much force is generated by output piston

is Pascal's Law

Formula :-

$$Force = pressure \times Area$$

$$pressure = \frac{Force}{Area}$$

$$Area = \frac{Force}{pressure}$$

Example :-



$$Piston Area = \frac{1}{2} \text{ in}^2$$

$$pressure = \frac{Force}{Area} = \frac{F}{A}$$

$$F = 5 \text{ lb}$$

$$A = \frac{1}{2} \text{ in}^2$$

$$5 \times \frac{2}{1} = 10 \text{ psi}$$

Example: ??

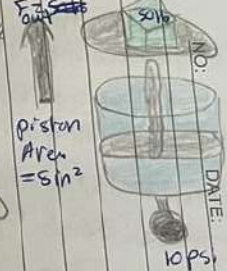
What's Force

$$P = 10 \text{ psi}$$

$$A = 5 \text{ in}^2$$

$$F = 10 \times 5$$

$$= 50 \text{ lb}$$



$$R_{in} = 30 \text{ in}$$

$$A_{in} = \frac{1}{4} \text{ in}^2$$

First part

$$A_{in} \cdot D = A_{out} \cdot D$$

$$\frac{1}{4} \cdot 30 = 15 \cdot D$$

$$\frac{30}{4} = 15D$$

$$7.5 = 15D$$

$$D = \frac{7.5}{15} = \frac{1}{2} \text{ in}$$

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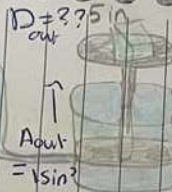
$$D = \frac{1}{2} \text{ in}$$

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$$D = \frac{1}{2} \text{ in}$$



Second part

$$P = \frac{\text{Force}}{\text{Area}}$$

$$= \frac{50 \text{ in} \cdot 50 \text{ lb}}{1/4} = 200 \text{ psi}$$

Third part

$$F = \text{Pressure} \times \text{Area}$$

$$= 200 \times 15 = 3000 \text{ lb}$$

Fourth part

$$MA = \frac{F_{out}}{F_{in}}$$

$$= \frac{3000}{50} = 60$$

$$MA = 60$$

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1. gases are compressible
liquids are incompressible

3. In normal temperature and pressure condition volume or density of gas doesn't change. However they can easily have small change in temperature or pressure

2. The main difference between compressible and incompressible when a force applied to a compressible changes density while when force applied to an incompressible doesn't change it meaning full degree.

1. curved surface enable the possibility of smooth flow with is free from turbulence.
2. Fluid particles able to speed up to negotiate the obstacle smoothly without turbulences.
3. This smooth flow is essential for low pressure development on the upper surface of a wing

Known as Streamlining, gradual shaping of areas where fluids must flow reduces the compression of gases and temperature of liquids in areas where turbulent flow may otherwise result

At molecular level :-

when pressure is applied on a gas, it affects gas in all direction, causing molecules to collide with greater frequency.

This collisions

1. give more time for the gas molecules to interact
2. more attraction force occur between molecules

These attraction force reduce motion of gas molecules

Compressibility:

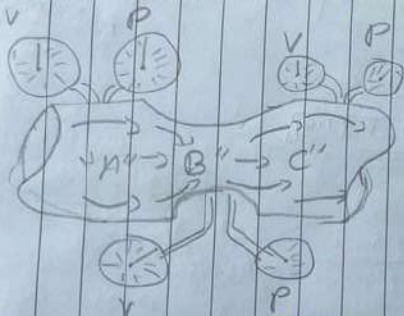
→ is a measure of how much volume of fluid change as a response of pressure change.

Streamlining :-

When a fluid encounters a particular obstacle it flows around it, even the wing of the aircraft or curved in hydraulic system line

Bernoulli's principle:

1. explain the action of a liquid flowing through the varying cross sectional areas of tubes.
2. A tube is shown the cross sectional area gradually decreases to a minimum diameter in its center section.
3. A tube constructed in this manner is called a "venturi" or venturi tube.



1. Cross sectionally the passageway referred to as converging duct.
2. As passageway starts to spread out is referred to as diverging duct.

dynamic pressure is associated with KE in the airflow.

Total pressure = Static pressure + Dynamic pressure



$$P_t = P_1 + \frac{1}{2} \rho_1 V_1^2 = P_2 + \frac{1}{2} \rho_2 V_2^2$$

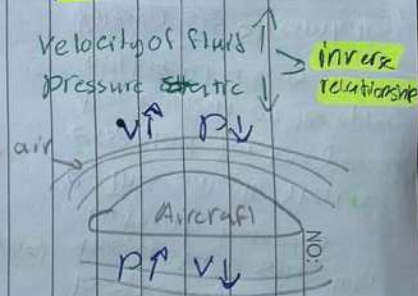
$P_2 < P_1$

total pressure

The Venturi is used to illustrate Bernoulli's principle which states:-

The static pressure of fluid (liquid or gas) ↓ P at point where

The velocity of fluid ↑ V provided no energy is added nor taken away from fluid. The velocity of the air is KE and static pressure of air is PE.



the total pressure of air flow remain the same

→ static pressure ↓
→ dynamic pressure ↑

Formulas :-

Center of gravity (CG)

$$\sum M_i = W_1 d_1 + W_2 d_2 + W_3 d_3 + W_4 d_4$$

$$\sum W_i = W_1 + W_2 + W_3 + W_4$$

$$CG = \frac{\sum M}{\sum W} = \frac{\text{total moment}}{\text{total weight}}$$

$$CG = \frac{W_1 d_1 + W_2 d_2 + W_3 d_3 + W_4 d_4}{W_1 + W_2 + W_3 + W_4}$$

Speed and velocity :-

$$S = \frac{d}{t}$$

$$V = \frac{d}{t} \text{ with direction}$$

↓

it can be

m/h or ft/s

convert m/h to
ft/s multiply x 1.467

Newton Second law:

$$F = \frac{W(V_f - V_i)}{gt} \quad / \quad F = ma$$

$$m = \frac{W}{g}$$

Centripetal Force :-

$$F_c = \frac{mv^2}{r}$$

Vibration

Frequency : / period :

$$f = \frac{1}{T}$$

$$T = \frac{1}{f}$$

$$T = 2\pi \sqrt{\frac{m}{g}}$$

periodic motion" pendulum "

$$T = 2\pi \sqrt{\frac{L}{g}}$$

32.2 ft/s² or 9.8 m/s²

moment:

$$W \cdot A \rightarrow \text{Arm}$$

$$M = W \cdot A \text{ OR } M = W \cdot d$$

unit of moment $\Rightarrow$ in-lb

Buoyancy :-

$$B = V \cdot \rho$$

↓
density

$B > W$
will float

$B < W$
will sink

Acceleration:

$$A = \frac{V_f - V_i}{t} \text{ acceleration due to gravity}$$

32.2 ft/s² (9.8 m/s²)

Velocity ratios-

$$\text{velocity ratio} = \frac{\text{distance moved by effort}}{\text{distance moved by load}}$$

gear ratio

$$\frac{\text{Teeth (of first object)}}{\text{teeth (of second object)}} = \frac{\text{Speed (of second object)}}{\text{Speed (of first object)}}$$

rpm
rpm

Efficiency

$$\text{Efficiency} = \frac{\text{MA}}{\text{Speed ratio}} \times 100$$

measured in %

Another way

$$\text{Efficiency} = \frac{\text{Measured performance}}{\text{ideal performance}}$$

Pascal's Law

$$\text{Force} = \text{Pressure} \times \text{Area}$$

unit $\swarrow$ $\swarrow$ $\downarrow$
lb psi in²

$$F = P \cdot A$$

$$\text{Pressure} = \frac{\text{Force}}{\text{Area}}$$

$$\text{Area} = \frac{\text{Force}}{\text{Pressure}}$$



Mechanical Advantage

$$\text{MA} = F_{\text{out}} \cdot D_{\text{out}} = F_{\text{in}} \cdot D_{\text{in}}$$

lb or N it depends $\rightarrow$ $= \frac{F_{\text{out}}}{F_{\text{in}}} = \frac{D_{\text{in}}}{D_{\text{out}}}$

Gears:

$$\frac{\text{Effort arm}}{\text{Resistance arm}} = \frac{F_{\text{out}}}{F_{\text{in}}}$$

density

$$\text{density} = \frac{\text{Weight}}{\text{Volume}}$$

imperial system $\rightarrow$ lb/ft³ or g/cm³
~~metric~~ ft³
metric system $\rightarrow$ cm³

two piston hydraulic system

input piston Area (Distance moved) = output piston Area (Distance moved)

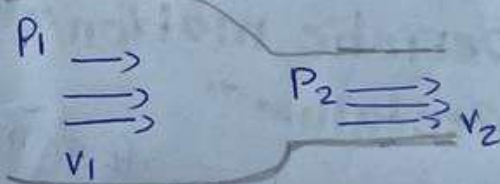
$$A_{\text{in}} \cdot D = A_{\text{out}} \cdot D$$

this shows

$$\text{Volume}_{\text{in}} = \text{Volume}_{\text{out}}$$

Bernoulli's principle

Total pressure = static pressure + Dynamic pressure



$$P_t = P_1 + \frac{1}{2} \rho_1 v_1^2 = P_2 + \frac{1}{2} \rho_2 v_2^2$$

total pressure

$$P_2 < P_1$$